Design and Analysis of Algorithms CSE 4th Sem (PCC CS 404)

Module 1 1.What is the time (a) O(n)	e complexity of insert(in	ndex) method in Arra	ayList	(d)O(logn)
2.Space complexity	(0) O(1)	aximum amount of _	requirec	by it during
(a)Time	(b)operation	(c)Memory Space	(d) None of	these
3.Frequently, the n the statement is Tr (a)True	nemory space required by rue or False or Maybe. (b) False	y an algorithm is a mu (c) May be	ltiple of the si (d) None of t	ze of input. State if hese
4.To verify whethe asymptotic or matl (a)Big Omega Ω (f)	r a function grows faster nematical notations, whic (b) Big Theta θ (f)	or slower than the oth h is (c)Big Oh O (f)	ner function, w	ve have some ll of these
5. Which of the give f1, f2, f3 and f4? f1 (a) f3, f2, f1, f4	en options provides the ii (n) = 2^n, f2(n) = n^(3/2) ,f (b)f2, f3, f1, f4	ncreasing order of asy f3(n) = nLogn ,f4(n) = r (c) f2, f3, f4, f1	mptotic comp/ (Logn) Select (d) f3,	olexity of functions t one: . f2, f4, f1
6. Which case of M (a) Case 3	aster's theorem is applica (b) Case 1 (c)N	able in the recurrence laster's theorem is no	relation T(n)= t applicable Co	0.5*T(n/2)+1/n? orrect (d)Case 2
7. Define the imple (a) abstract level	mentation level 0f data s (b)implementation	tructure? n level (c) appli	ication level	(d)none of these
8.ln computer sci solution to a prob (a) True	ence, algorithm refers t blem.	o a special method u	usable by a co (b) F	omputer for the alse
9.Which of the fol Algorithms can be (a) as pseudo cod	lowing is incorrect? e represented: es (b) as synta	x (c) as pro	ograms	(d) as flowcharts
10 com (a) (n 2 + n + 2) / 2	parisons required to so (b) (n³ + n – 2) / 2	rt the list 1, 2, 3r (c) (n²+ n – 2)	n using insert	ion sort.) (n²– n – 2) / 2
11. The complexit (a) O(2 [°])	y of Fibonacci series is ₋ b) O(log n)	(c) O(r	J ²)	(d) O(n log n)
12.The big-theta ı (a) n²logn	notation for f(n) = nlog(r (b) n ²	י² + 1) + n²logn is? (c) logn	1	(d) nlog(n²)
13.Master's theor (a) T (n) = 2T (n/2 (c) T (n) = T (n-2)	rem can be applied on v 2) + 2^n + 2n^2 + 1	which of the followir (b) T (d) N	ig recurrence (n) = 2T (n/3) one of these	relation?) + sin(n)

 $\begin{array}{ll} 14.T(n) = 3T(n/2+47) + 2n^{2} + 10^{*}n - 1/2. \ T(n) \ \text{will be} \\ (a) \ O(n^{2}) \qquad (b) \ O(n^{*}(3/2)) \qquad (c) \ O(n \ \text{log } n) \qquad (d) \ \text{None of these} \end{array}$

15.Solve the following recurrence equation T(n) = 2T(n/2) + n.

16. Solve using Substitution Method $T(n) = T(\sqrt{n}) + 1$

17. Represent in O notation of following recurrence equation $T(n) = 2T(n/2) + \sqrt{n}$.

- 18. State Master Theorem with example.
- 19. Write a recurrence for the running time of g(n), and solve that recurrence. Assume that addition can be done in constant time.

```
def g(n):
```

if n == 1: return 1 else: x = g(n-1) return x+x

20. Now assume addition takes time $\Theta(b)$ where b is the number of bits in the larger number. Write a new recurrence for the running time of g(n), and solve that recurrence. Express your final answer in Θ -notation.

Module 2

1. Where is linear searching used?

(a) When the list has only a few elements

(b) When performing a single search in an unordered list

(c) Used all the time

(d) When the list has only a few elements and When performing a single search in an unordered list

2. What is the best case and worst case complexity of ordered linear search?(a) O(nlogn), O(logn)(b) O(logn), O(nlogn)(c) O(n), O(1)(d) O(1), O(n)

3. In which of the cases uniform binary search fails compared to binary search?

(a) A table lookup is generally faster than an addition and a shift

(b) Many searches will be performed on the same array

(c) Many searches will be performed on several arrays of the same length

(d) Complexity of code

4. Given, arr = {1,3,5,6,7,9,14,15,17,19} key = 17 and delta = {5,3,1,0}
How many key comparisons are made?(exclude the comparison used to decide the left or right sub array)

(a) 4 (b) 3 (c) 5 (d) 6

5. What will be the auxiliary space complexity of the following code? #include<bits/stdc++.h>

```
using namespace std;
void func(char* str2, char* str1)
{
         int m = strlen(str2);
         int n = strlen(str1);
         for (int i = 0; i <= n - m; i++)</pre>
         {
                   int j;
                   for (j = 0; j < m; j++)
                            if (str1[i + j] != str2[j])
                                      break;
                   if (j == m)
                            cout << i << endl;</pre>
         }
}
int main()
{
         char str1[] = "1253234";
         char str2[] = "323";
         func(str2, str1);
         return 0;
}
(a) O(n)
                          (b) O(1)
                                                            (c) O(log n)
                                                                                     (d) O(m)
```

6. Which of the following is correct with regard to insertion sort?

- (a) insertion sort is stable and it sorts In-place
- (b) insertion sort is unstable and it sorts In-place

(c) insertion sort is stable and it does not sort In-place

(d) insertion sort is unstable and it does not sort In-place

7. The worst case time complexity of insertion sort is $O(n_2)$. What will be the worst case time
complexity of insertion sort if the correct position for inserting element is calculated using
binary search?(a) O(nlogn)(b) $O(n^2)$ (c) O(n)(d) O(logn)

8. Which of the following sorting algorithm is best suited if the elements are already sorted?(a) Heap Sort(b) Quick Sort(c) Insertion Sort(d) Merge Sort

9. What is an extern(a) Algorithm that us(b) Algorithm that us(c) Algorithm that inv(d) Algorithm that are	al sorting algorithm? es tape or disk during th es main memory during olves swapping e considered 'in place'	ie sort the sort	
10. What is the worst	t case complexity of bub	ble sort?	(d) O(n ²)
(a) O(nlogn)	(b) O(logn)	(c) O(n)	
11. What is the wors	t case time complexity o	of merge sort?	(d) O(n log n²)
(a) O(n log n)	(b) O(n²)	(c) O(n² log n)	
12. What is the avera	ge case complexity of Q	uickSort?	(d) O(n²)
(a) O(nlogn)	(b) O(logn)	(c) O(n)	
13. What is the best	case time complexity ra	ndomized quick sort?	(d) O(n² log n)
(a) O(log n)	(b) O(n log n)	(c) O(n²)	
14. What is the med (a) quick sort with ra (b) quick sort with ra (c) choosing median (d) choosing median	ian of three techniques ndom partitions ndom choice of pivot element as pivot of first, last and middle	in quick sort? element as pivot	
15. How many elem	ents can be sorted in O(logn) time using Heap sort	?
(a) O(1)	(b) O(n/2)	(c) O(logn/log(logn))	(d) O(logn)
16. Analyze the time 17. Give Strassen's M 18. Suppose we are s finished some heapit like this: 16 14 15 10 performed on root o 19. Describe Divide a 20. Give algorithm a	complexity of quick sort latrix Multiplication algo sorting an array of eight fy (either maxheapify or 12 27 28. Compute num f heap? Ind conquor paradigm w nd comparision of Linea	using recurrence equation rithm. integers using heapsort, an minheapify) operations. Th ber of heapify operations vith example. Ir Search and Binary Search	n. nd we have just ne array now looks have been n.
Module 3 1.Which of the follow (a) exhaustive search (c) brute force algorit	ving algorithms is the be n thm	st approach for solving Hu (b) greedy al (d) divide and	ffman codes? gorithm d conquer algorithm
2. What is the runnin	g time of the Huffman e	encoding algorithm?	(d) O(N log C)
(a) O(C)	(b) O(log C)	(c) O(C log C)	

3.What is the runnir queue is done using	ng time of the Huffman algo g linked lists?	rithm, if its implementa	tion of the priority
(a) O(C)	(b) O(log C)	(c) O(C log C)	(d) O(C ²)
4.Which of the follo correct?	wing statement about 0/1 kr	napsack and fractional k	knapsack problem is
(a) In 0/1 knapsack j indivisible (b) Both are the san	problem items are divisible a	and in fractional knapsa	ick items are
(c) 0/1 knapsack is s dynamic programm (d) In 0/1 knapsack	olved using a greedy algorit ling problem items are indivisibl	hm and fractional knap e and in fractional knap	sack is solved using sack items are
divisible			
5.Time complexity c (a) O(n log n)	of fractional knapsack proble (b) O(n)	em is (c) O(n ²)	(d) O(nW)
6.Given items as {va Find the maximum	alue,weight} pairs {{40,20},{3 value output assuming item	30,10},{20,5}}. The capac s to be divisible.	ity of knapsack=20.
(a) 60	(b) 80	(c) 100	(d) 40
7.Given items as {va Find the maximum	alue,weight} pairs {{60,20},{5 value output assuming item	60,25},{20,5}}. The capac s to be divisible and no	tity of knapsack=40. ndivisible
(a) 100, 80	(b) 110, 70	(c) 130, 110	(d) 110, 80
8.Which of the follo (a) Optimal substrue (c) Greedy approach	wing is/are property/proper cture า (d) Both optimal	ties of a dynamic progra (b) Overlapp l substructure and overl	amming problem? ing subproblems lapping subproblems
9.Which of the follo	wing problems is NOT solve	d using dynamic progra	mming?
(a) 0/1 knapsack pro (c) Edit distance pro	blem	(b) Matrix chain m (d) Fractional kna	ultiplication problem psack problem
10.You are given a k weights {20, 30, 40, items you can carry	(napsack that can carry a ma 70} and values {70, 80, 90, 2 using the knapsack?	aximum weight of 60. Th 200}. What is the maxim	nere are 4 items with um value of the
(a) 160	(b) 200	(c) 170	(d) 90
11.Consider the ma respectively. What is	trices P, Q and R which are 1 s the minimum number of n	10 x 20, 20 x 30 and 30 > nultiplications required	< 40 matrices to multiply the three
matrices?	(1) 12000	() 24022	

(a) 18000 (b) 12000 (c) 24000 (d) 32000

```
12.Which of the following is the recurrence relation for the matrix chain multiplication
problem where mat[i-1] * mat[i] gives the dimension of the ith matrix?
(a) dp[i,j] = 1 if i=j
dp[i,j] = min{dp[i,k] + dp[k+1,j]}
(b) dp[i,j] = 0 if i=j
dp[i,j] = min{dp[i,k] + dp[k+1,j]}
(c) dp[i,j] = 1 if i=j
dp[i,j] = min{dp[i,k] + dp[k+1,j]} + mat[i-1]*mat[k]*mat[j].
(d) dp[i,j] = 0 if i=j
dp[i,j] = min{dp[i,k] + dp[k+1,j]} + mat[i-1]*mat[k]*mat[j].
```

```
      13.Find the length of the longest increasing subsequence for the given sequence:

      {-10, 24, -9, 35, -21, 55, -41, 76, 84}

      (a) 5
      (b) 4
      (c) 3
      (d) 6
```

14.Given a rod of length n and the selling prices of all pieces smaller than equal to n, find the most beneficial way of cutting the rod into smaller pieces. This problem is called the rod cutting problem. Which of these methods can be used to solve the rod cutting problem? (a) Brute force

(b) Dynamic programming

(c) Recursion

(d) Brute force, Dynamic programming and Recursion

15. Which of the following is an application of the edit distance problem?

(a) Approximate string matching

(b) Spelling correction

(c) Similarity of DNA

(d) Approximate string matching, Spelling Correction and Similarity of DNA

16. Differentiate among Divide and conquor, Greedy and Dynamic Programming paradigm.

17. Describe Travelling Salesman Problem.

18. Give the algorithm to compute Fibonacci series using Dynamic programming approach and compare with other approach.

19. Describe Bin packing problem with the help of numerical example.

20. Describe characteristics of Dynamic Programming.

Module 4

1. Depth First Search is equivalent to which of the travers	sal in the Binary Trees?
(a) Pre-order Traversal	(b) Post-order Traversal
(c) Level-order Traversal	(d) In-order Traversal

2.Time Complexity of DFS is? (V – number of vertices, E – number of edges)(a) O(V + E)(b) O(V)(c) O(E)(d) O(V*E)

 3. Which of the follow (a) For generating top (b) For generating Str (c) Detecting cycles in (d) Peer to Peer Network 	ving is not an applicat pological sort of a gra rongly Connected Cor n the graph vorks	tion of Depth First Searc ph nponents of a directed	ch? graph
4.Breadth First Searc (a) Pre-order Travers (c) Level-order Traver	h is equivalent to whi al rsal	ch of the traversal in th (b) (d)	e Binary Trees? Post-order Traversal In-order Traversal
5.Time Complexity of (a) O(V + E)	Breadth First Search (b) O(V)	is? (V – number of verti (c) O(E)	ces, E – number of edges) (d) O(V*E)
6.Which of the follow (a) It is tree that span (c) It includes every v	ring is false in the case is G ertex of the G	e of a spanning tree of a (b) It is a (d) It can	a graph G? subgraph of the G be either cyclic or acyclic
7.Which of the follow (a) The spanning tree (b) MST have n – 1 ed (c) Edge e belonging t the same cut, then th (d) Removing one edge	ring is false? es do not have any cyc lges if the graph has r to a cut of the graph i ne edge e is present ir ge from the spanning	cles n edges f has the weight smalle n all the MSTs of the gra ; tree will not make the g	r than any other edge in ph graph disconnected
8.What is the time co (a) O(log V)	mplexity of Kruskal's (b) O(E log V)	algorithm? (c) O(E ²)	(d) O(V log E)
9.Consider the follow S1. Kruskal's algorithe S2. Kruskal's algorithe (a) S1 is true but S2 is (c) Both S1 and S2 are	<i>v</i> ing statements. m might produce a no m can efficiently impl s false e true	on-minimal spanning tro emented using the disjo (b) (d	ee. oint-set data structure.) Both S1 and S2 are false)) S2 is true but S1 is false
10. Worst case is the used?	worst case time com	plexity of Prim's algorith	nm if adjacency matrix is
(a) O(log V)	(b) O(V ²)	(c) O(E ²)	(d) O(V log E)
11.Which of the follow (a) It is a greedy algor (b) It constructs MST (c) It never accepts cy (d) It can be impleme	wing is false about Pr rithm by selecting edges in rcles in the MST ented using the Fibona	im's algorithm? increasing order of thei acci heap	ir weights
12.Dijkstra's Algorith (a) Directed and weig (c) Unweighted graph	m cannot be applied o hted graphs	on (b) Graphs havin (d) Undirected a	g negative weight function and unweighted graphs

13. What is running tir (a) O(V)	ne of Dijkstra's algorithn (b) O(VlogV)	n using Binary min (c) O(E)	- heap method? (d) O(ElogV)
14.Dijkstra's Algorithm (a) Greedy algorithm (c) Back tracking	is the prime example fo	or (t	o) Branch and bound d) Dynamic programming
15.Bellmann Ford Algo (a) Undirected and we (c) Directed and weigh	orithm can be applied fo ighted graphs ted graphs	r(b) Undirec (d) All direc	ted and unweighted graphs ted graphs
16. Floyd Warshall Algo (a) Single source short (c) Minimum spanning	orithm can be used for f est path ; tree	inding((_ b) Topological sort d) Transitive closure
17. With the help of nuBellman Ford algorithm18.Give the algorithm19. Using strong argundisconnected.20. What is strongly compared to the strong stro	umerical example differe m. to find MST using Kurska nnet show that the a gar onnected component and	entiate between Di al's algorithm. rph having less the d give its algorithm	jkstra's algorithm and en n-1 edges is n to find it?
Module 5			
1.The worst-case effici (a) O(p(n))	ency of solving a proble (b) O(p(n log n))	m in polynomial tiı (c) O(p(n²))	me is? (d) O(p(m log n))
2.Problems that can b (a) intractable	e solved in polynomial ti (b) tractable	me are known as? (c) decision	(d) complete
3 is the class	of decision problems th	at can be solved b	y non-deterministic
(a) NP	(b) P	(c) Hard	(d) Complete
4.Problems that canno (a) tractable problems (c) undecidable proble	ot be solved by any algor ms	ithm are called? (k (c	o) intractable problems l) decidable problems
5. To which class does (a) P class	the Euler's circuit proble (b) NP class	em belong? (c) Partition class	(d) Complete class
6. Halting problem is a (a) decidable problem (c) complete problem	in example for?		(b) undecidable problem (d) trackable problem

7. How many conditions have to be met if an NP- complete problem is polynomially reducible? (a) 1 (b) 2 (c) 3 (d) 4 8.To which of the following class does a CNF-satisfiability problem belong? (a) NP class (b) P class (c) NP complete (d) NP hard 9. Which of the following problems is not NP complete? (a) Hamiltonian circuit (b) Bin packing (c) Partition problem (d) Halting problem 10. The choice of polynomial class has led to the development of an extensive theory called (a) computational complexity (b) time complexity (c) problem complexity (d) decision complexity 11.Hamiltonian path problem is _____ (a) NP problem (b) N class problem (c) P class problem (d) NP complete problem 12. Subset sum problem is an example of NP-complete problem. (a) true (b) false 13. What is a subset sum problem? (a) finding a subset of a set that has sum of elements equal to a given number (b) checking for the presence of a subset that has sum of elements equal to a given number and printing true or false based on the result (c) finding the sum of elements present in a set (d) finding the sum of all the subsets of a set 14.What is the set partition problem? (a) finding a subset of a set that has sum of elements equal to a given number (b) checking for the presence of a subset that has sum of elements equal to a given number (c) checking whether the set can be divided into two subsets of with equal sum of elements and printing true or false based on the result (d) finding subsets with equal sum of elements 15.Set partition problem is an example of NP complete problem. (a) true (b) false 16. Describe optimization and decision problem. 17. Describe P and NP – class problem. 18. State Cook's Theorem. 19. Explain the different ways to analyze randamize algorithm. 20. Explain the need of approximation algorithm.

Darbhanga College of Engineering Darbhanga

Midterm Exam, March 2020

Design & Analysis of Algorithm (CSE 4th Sem)

Duration: 2 Hrs Regestration No:

Max Marks : 20

Instruction:

1. If any rough work found on question paper during examination, invigilator can deduct 5 marks.

2. Attempt all questions. No any clarification related to question will be entertained, If you are considering any assumption must mention it.

S.	Questions	Marks	$\rm CO^1$	BL^2
No				
1.	Solve the recurrence $T(n) = 2T(n/4) + \sqrt{n}$	4	CO1	L1
	OB			
	Apply Master theorm on following recurrence			
	The probability of the probabil			
	a. $T(n) = 3T(n/3) + n$ b. $T(n) = 3T(n/4) + n \log n$			
2	5. $1(n) = 51(n/4) + n \log n$	4	CO1	L2
2.	show that: $a \log(1n) - \Theta(n \log n)$	т	001	112
	a. $\log(n) = O(n \log n)$.			
	b. For any real coonstants a and b, $b \ge 1$ and $(n+a)^{\circ} = \Theta(n^{\circ})$			
	OR			
	a. Solve the recurrence $T(n) = T(n-1) + 1/n$			
3.	Prove that, For any two function $f(n)$ and $g(n)$, we have $f(n) = \Theta(g(n))$	4	CO2	L5
	iff $f(n) = O(g(n))$ and $f(n) = \Omega(g(n))$.			
4.	For a given sequence analyze with reason which one will be time and space			
	efficient in the case of Insertion Sort, Quick Sort and Merge Sort.			
	Sequence $a : 1, 2, 3, 4, 5, \dots, 10$.			
	Sequence b : 10,9,8,,1.	4	CO3	L3
5.	Compute time complexity of Quick Sort in the best , average and worst	4	CO3	L5
	case.			

End

¹Course Outcome

²Bloom Level

DARBHANGA COLLEGE OF ENGINEERING, DARBHANGA Mid-Sem Examination

Design and Analysis of Algorithms

(CSE 5th Sem 051506)

Max Marks : 20 Max Time : 2 Hrs

Instruction:

Question number 1 to 8 carry equal marks and each having 5 marks, attempt any four from question number 1 to 8.

OR

Attempt only question number 9, it carry 20 marks.

1. Prove that either graphically or analytically $\Theta(g(n)) = O(g(n)) \cap \Omega(g(n))$.

2. Express following in terms of Θ notation, assume 'n' terms.

- a) $1 + 8 + 27 + 64 + \dots$
- b) log (!n), here !n represents factorial of n.

3. Compute the soluition of the following recurrence.

- a) T(n) = 5xT(n/5) + n / logn.
- b) $T(n) = 13246 \text{ x}T(n/68) + n^2$.

4. For a given sequence analyze with reason which one will be time and space efficient in the case of Insertion Sort, Quick Sort and Merge Sort.

Sequence a : 1,2,3,4,5....,10. Sequence b : 10,9,8,....,1.

5.

a. In the implementation of a priority queue, following operation takes what amount of time in O representation.

i. Insert ii Extract Minimum iii. Decrease Key. b. What will be the run time of Dijkstra algorithm using priority queue implementation.

6. Show that the second smallest of 'n ' elements can be found with $n + \lg n - 2$ comparisions in the worst case.

7. As shown in figure 1 for a given adjacency list representation of a graph, run topological sort on the graph. Answer should consist of a list of the vertices in a particular order

A	
В	
С	
D	
Е	
F	
G	

8.

Figure 1

a. Define the following terms with respect to time stamp.

i Tree Edge ii Forward Edge. iii Back Edge b. Show that a Graph is DAG iff it has no back edge. iv Cross Edge.

9. You are interested in analyzing some hard to obtain data from two separate databases. Each database contains 'n' numerical values – so there are 2n values total- and you may assume that no two values are the same. You'd like to determine the median of this set of 2n values, which we will define here to be the nth smallest value.

However, the only way you can access these values is through queries to the databases. In a single query, you can specify a value 'k' to one of the two databases, and the chosen database will return the kth smallest value that it contains. Since queries are expensive, you would like to compute the median using as few queries as possible.

Give an algorithm that finds the median value using at most O(log n) queries.

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4.To verify whethe asymptotic or matl (a)Big Omega Ω (f)	r a function grows faster nematical notations, whic (b) Big Theta θ (f)	or slower than the oth h is (c)Big Oh O (f)	ner function, w	ve have some ll of these
5. Which of the give f1, f2, f3 and f4? f1 (a) f3, f2, f1, f4	en options provides the ii (n) = 2^n, f2(n) = n^(3/2) ,f (b)f2, f3, f1, f4	ncreasing order of asy f3(n) = nLogn ,f4(n) = r (c) f2, f3, f4, f1	mptotic comp/ (Logn) Select/ (d) f3,	olexity of functions t one: . f2, f4, f1
6. Which case of M (a) Case 3	aster's theorem is applica (b) Case 1 (c)N	able in the recurrence laster's theorem is no	relation T(n)= t applicable Co	0.5*T(n/2)+1/n? orrect (d)Case 2
7. Define the imple (a) abstract level	mentation level 0f data s (b)implementation	tructure? n level (c) appli	ication level	(d)none of these
8.ln computer sci solution to a prob (a) True	ence, algorithm refers t blem.	o a special method u	usable by a co (b) F	omputer for the alse
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12.The big-theta ı (a) n²logn	notation for f(n) = nlog(r (b) n ²	י² + 1) + n²logn is? (c) logn	1	(d) nlog(n²)
13.Master's theor (a) T (n) = 2T (n/2 (c) T (n) = T (n-2)	rem can be applied on v 2) + 2^n + 2n^2 + 1	which of the followir (b) T (d) N	ig recurrence (n) = 2T (n/3) one of these	relation?) + sin(n)

 $\begin{array}{ll} 14.T(n) = 3T(n/2+47) + 2n^{2} + 10^{*}n - 1/2. \ T(n) \ \text{will be} \\ (a) \ O(n^{2}) \qquad (b) \ O(n^{*}(3/2)) \qquad (c) \ O(n \ \text{log } n) \qquad (d) \ \text{None of these} \end{array}$

15.Solve the following recurrence equation T(n) = 2T(n/2) + n.

16. Solve using Substitution Method $T(n) = T(\sqrt{n}) + 1$

17. Represent in O notation of following recurrence equation $T(n) = 2T(n/2) + \sqrt{n}$.

- 18. State Master Theorem with example.
- 19. Write a recurrence for the running time of g(n), and solve that recurrence. Assume that addition can be done in constant time.

```
def g(n):
```

if n == 1: return 1 else: x = g(n-1) return x+x

20. Now assume addition takes time $\Theta(b)$ where b is the number of bits in the larger number. Write a new recurrence for the running time of g(n), and solve that recurrence. Express your final answer in Θ -notation.

Module 2

1. Where is linear searching used?

(a) When the list has only a few elements

(b) When performing a single search in an unordered list

(c) Used all the time

(d) When the list has only a few elements and When performing a single search in an unordered list

2. What is the best case and worst case complexity of ordered linear search?(a) O(nlogn), O(logn)(b) O(logn), O(nlogn)(c) O(n), O(1)(d) O(1), O(n)

3. In which of the cases uniform binary search fails compared to binary search?

(a) A table lookup is generally faster than an addition and a shift

(b) Many searches will be performed on the same array

(c) Many searches will be performed on several arrays of the same length

(d) Complexity of code

4. Given, arr = {1,3,5,6,7,9,14,15,17,19} key = 17 and delta = {5,3,1,0}
How many key comparisons are made?(exclude the comparison used to decide the left or right sub array)

(a) 4 (b) 3 (c) 5 (d) 6

5. What will be the auxiliary space complexity of the following code? #include<bits/stdc++.h>

```
using namespace std;
void func(char* str2, char* str1)
{
         int m = strlen(str2);
         int n = strlen(str1);
         for (int i = 0; i <= n - m; i++)</pre>
         {
                   int j;
                   for (j = 0; j < m; j++)
                            if (str1[i + j] != str2[j])
                                      break;
                   if (j == m)
                            cout << i << endl;</pre>
         }
}
int main()
{
         char str1[] = "1253234";
         char str2[] = "323";
         func(str2, str1);
         return 0;
}
(a) O(n)
                          (b) O(1)
                                                            (c) O(log n)
                                                                                     (d) O(m)
```

6. Which of the following is correct with regard to insertion sort?

- (a) insertion sort is stable and it sorts In-place
- (b) insertion sort is unstable and it sorts In-place

(c) insertion sort is stable and it does not sort In-place

(d) insertion sort is unstable and it does not sort In-place

7. The worst case time complexity of insertion sort is $O(n_2)$. What will be the worst case time
complexity of insertion sort if the correct position for inserting element is calculated using
binary search?(a) O(nlogn)(b) $O(n^2)$ (c) O(n)(d) O(logn)

8. Which of the following sorting algorithm is best suited if the elements are already sorted?(a) Heap Sort(b) Quick Sort(c) Insertion Sort(d) Merge Sort

9. What is an extern(a) Algorithm that us(b) Algorithm that us(c) Algorithm that inv(d) Algorithm that are	al sorting algorithm? es tape or disk during th es main memory during olves swapping e considered 'in place'	ie sort the sort	
10. What is the worst	t case complexity of bub	ble sort?	(d) O(n ²)
(a) O(nlogn)	(b) O(logn)	(c) O(n)	
11. What is the wors	t case time complexity o	of merge sort?	(d) O(n log n²)
(a) O(n log n)	(b) O(n²)	(c) O(n² log n)	
12. What is the avera	ge case complexity of Q	uickSort?	(d) O(n²)
(a) O(nlogn)	(b) O(logn)	(c) O(n)	
13. What is the best	case time complexity ra	ndomized quick sort?	(d) O(n² log n)
(a) O(log n)	(b) O(n log n)	(c) O(n²)	
14. What is the med (a) quick sort with ra (b) quick sort with ra (c) choosing median (d) choosing median	ian of three techniques ndom partitions ndom choice of pivot element as pivot of first, last and middle	in quick sort? element as pivot	
15. How many elem	ents can be sorted in O(logn) time using Heap sort	?
(a) O(1)	(b) O(n/2)	(c) O(logn/log(logn))	(d) O(logn)
16. Analyze the time 17. Give Strassen's M 18. Suppose we are s finished some heapit like this: 16 14 15 10 performed on root o 19. Describe Divide a 20. Give algorithm a	complexity of quick sort latrix Multiplication algo sorting an array of eight fy (either maxheapify or 12 27 28. Compute num f heap? Ind conquor paradigm w nd comparision of Linea	using recurrence equation rithm. integers using heapsort, an minheapify) operations. Th ber of heapify operations vith example. Ir Search and Binary Search	n. nd we have just ne array now looks have been n.
Module 3 1.Which of the follow (a) exhaustive search (c) brute force algorit	ving algorithms is the be n thm	st approach for solving Hu (b) greedy al (d) divide and	ffman codes? gorithm d conquer algorithm
2. What is the runnin	g time of the Huffman e	encoding algorithm?	(d) O(N log C)
(a) O(C)	(b) O(log C)	(c) O(C log C)	

3.What is the runnir queue is done using	ng time of the Huffman algo g linked lists?	rithm, if its implementa	tion of the priority
(a) O(C)	(b) O(log C)	(c) O(C log C)	(d) O(C ²)
4.Which of the follo correct?	wing statement about 0/1 kr	napsack and fractional k	knapsack problem is
(a) In 0/1 knapsack j indivisible (b) Both are the san	problem items are divisible a	and in fractional knapsa	ick items are
(c) 0/1 knapsack is s dynamic programm (d) In 0/1 knapsack	olved using a greedy algorit ling problem items are indivisibl	hm and fractional knap e and in fractional knap	sack is solved using sack items are
divisible			
5.Time complexity c (a) O(n log n)	of fractional knapsack proble (b) O(n)	em is (c) O(n ²)	(d) O(nW)
6.Given items as {va Find the maximum	alue,weight} pairs {{40,20},{3 value output assuming item	30,10},{20,5}}. The capac s to be divisible.	ity of knapsack=20.
(a) 60	(b) 80	(c) 100	(d) 40
7.Given items as {va Find the maximum	alue,weight} pairs {{60,20},{5 value output assuming item	60,25},{20,5}}. The capac s to be divisible and no	tity of knapsack=40. ndivisible
(a) 100, 80	(b) 110, 70	(c) 130, 110	(d) 110, 80
8.Which of the follo (a) Optimal substrue (c) Greedy approach	wing is/are property/proper cture า (d) Both optimal	ties of a dynamic progra (b) Overlapp l substructure and overl	amming problem? ing subproblems lapping subproblems
9.Which of the follo	wing problems is NOT solve	d using dynamic progra	mming?
(a) 0/1 knapsack pro (c) Edit distance pro	blem	(b) Matrix chain m (d) Fractional kna	ultiplication problem psack problem
10.You are given a k weights {20, 30, 40, items you can carry	(napsack that can carry a ma 70} and values {70, 80, 90, 2 using the knapsack?	aximum weight of 60. Th 200}. What is the maxim	nere are 4 items with um value of the
(a) 160	(b) 200	(c) 170	(d) 90
11.Consider the ma respectively. What is	trices P, Q and R which are 1 s the minimum number of n	10 x 20, 20 x 30 and 30 > nultiplications required	< 40 matrices to multiply the three
matrices?	(1) 12000	() 24022	

(a) 18000 (b) 12000 (c) 24000 (d) 32000

```
12.Which of the following is the recurrence relation for the matrix chain multiplication
problem where mat[i-1] * mat[i] gives the dimension of the ith matrix?
(a) dp[i,j] = 1 if i=j
dp[i,j] = min{dp[i,k] + dp[k+1,j]}
(b) dp[i,j] = 0 if i=j
dp[i,j] = min{dp[i,k] + dp[k+1,j]}
(c) dp[i,j] = 1 if i=j
dp[i,j] = min{dp[i,k] + dp[k+1,j]} + mat[i-1]*mat[k]*mat[j].
(d) dp[i,j] = 0 if i=j
dp[i,j] = min{dp[i,k] + dp[k+1,j]} + mat[i-1]*mat[k]*mat[j].
```

```
      13.Find the length of the longest increasing subsequence for the given sequence:

      {-10, 24, -9, 35, -21, 55, -41, 76, 84}

      (a) 5
      (b) 4
      (c) 3
      (d) 6
```

14.Given a rod of length n and the selling prices of all pieces smaller than equal to n, find the most beneficial way of cutting the rod into smaller pieces. This problem is called the rod cutting problem. Which of these methods can be used to solve the rod cutting problem? (a) Brute force

(b) Dynamic programming

(c) Recursion

(d) Brute force, Dynamic programming and Recursion

15. Which of the following is an application of the edit distance problem?

(a) Approximate string matching

(b) Spelling correction

(c) Similarity of DNA

(d) Approximate string matching, Spelling Correction and Similarity of DNA

16. Differentiate among Divide and conquor, Greedy and Dynamic Programming paradigm.

17. Describe Travelling Salesman Problem.

18. Give the algorithm to compute Fibonacci series using Dynamic programming approach and compare with other approach.

19. Describe Bin packing problem with the help of numerical example.

20. Describe characteristics of Dynamic Programming.

Module 4

1. Depth First Search is equivalent to which of the travers	sal in the Binary Trees?
(a) Pre-order Traversal	(b) Post-order Traversal
(c) Level-order Traversal	(d) In-order Traversal

2.Time Complexity of DFS is? (V – number of vertices, E – number of edges)(a) O(V + E)(b) O(V)(c) O(E)(d) O(V*E)

 3. Which of the follow (a) For generating to (b) For generating St (c) Detecting cycles in (d) Peer to Peer Network 	wing is not an applicat pological sort of a gra rongly Connected Con n the graph vorks	ion of Depth First Search? ph nponents of a directed gra	aph		
4.Breadth First Searc (a) Pre-order Travers (c) Level-order Trave	:h is equivalent to whi al rsal	ch of the traversal in the E (b) Po (d) In·	of the traversal in the Binary Trees? (b) Post-order Traversal (d) In-order Traversal		
5.Time Complexity o (a) O(V + E)	f Breadth First Search (b) O(V)	is? (V – number of vertices (c) O(E)	s, E – number of edges) (d) O(V*E)		
6.Which of the follow (a) It is tree that spar (c) It includes every v	ving is false in the case is G vertex of the G	e of a spanning tree of a gi (b) It is a sub (d) It can be	raph G? ograph of the G e either cyclic or acyclic		
7.Which of the follow (a) The spanning tree (b) MST have n – 1 ec (c) Edge e belonging the same cut, then th (d) Removing one ed	ving is false? es do not have any cyc dges if the graph has r to a cut of the graph i ne edge e is present ir ge from the spanning	cles n edges f has the weight smaller th n all the MSTs of the graph tree will not make the gra	nan any other edge in aph disconnected		
8.What is the time co (a) O(log V)	omplexity of Kruskal's (b) O(E log V)	algorithm? (c) O(E ²)	(d) O(V log E)		
9.Consider the follow S1. Kruskal's algorith S2. Kruskal's algorith (a) S1 is true but S2 i (c) Both S1 and S2 ar	ving statements. Im might produce a no Im can efficiently imple s false re true	on-minimal spanning tree. emented using the disjoin (b) Bo (d) S	t-set data structure. oth S1 and S2 are false 2 is true but S1 is false		
10. Worst case is the used?	worst case time comp	plexity of Prim's algorithm	if adjacency matrix is		
(a) O(log V)	(b) O(V ²)	(c) O(E ²)	(d) O(V log E)		
 (a) It is a greedy algo (b) It constructs MST (c) It never accepts constructed in the second s	wing is false about Pri rithm by selecting edges in ycles in the MST ented using the Fibona	im's algorithm? increasing order of their v acci heap	veights		
12.Dijkstra's Algorith (a) Directed and weig (c) Unweighted grapl	m cannot be applied o ghted graphs hs	on (b) Graphs having r (d) Undirected and	negative weight function d unweighted graphs		

13. What is running tir (a) O(V)	ne of Dijkstra's algorithn (b) O(VlogV)	n using Binary min (c) O(E)	- heap method? (d) O(ElogV)	
14.Dijkstra's Algorithm (a) Greedy algorithm (c) Back tracking	is the prime example fo	or (b (b	o) Branch and bound d) Dynamic programming	
15.Bellmann Ford Algo (a) Undirected and we (c) Directed and weigh	orithm can be applied for ighted graphs ted graphs	r(b) Undirec (d) All direc	ted and unweighted graphs ted graphs	
16. Floyd Warshall Algo (a) Single source short (c) Minimum spanning	orithm can be used for f est path ; tree	inding((_ b) Topological sort d) Transitive closure	
 17. With the help of numerical example differentiate between Dijkstra's algorithm and Bellman Ford algorithm. 18.Give the algorithm to find MST using Kurskal's algorithm. 19. Using strong argumnet show that the a garph having less then n-1 edges is disconnected. 20. What is strongly connected component and give its algorithm to find it? 				
Module 5				
1.The worst-case effici (a) O(p(n))	ency of solving a proble (b) O(p(n log n))	m in polynomial tir (c) O(p(n²))	me is? (d) O(p(m log n))	
2.Problems that can b (a) intractable	e solved in polynomial ti (b) tractable	me are known as? (c) decision	(d) complete	
3 is the class	of decision problems th	at can be solved b	y non-deterministic	
(a) NP	(b) P	(c) Hard	(d) Complete	
4.Problems that cannot be solved by any algorith (a) tractable problems (c) undecidable problems		hm are called? (b) intractable problems (d) decidable problems		
5. To which class does (a) P class	the Euler's circuit proble (b) NP class	em belong? (c) Partition class	(d) Complete class	
6. Halting problem is an example for? (a) decidable problem (c) complete problem			(b) undecidable problem (d) trackable problem	

7. How many conditions have to be met if an NP- complete problem is polynomially reducible? (a) 1 (b) 2 (c) 3 (d) 4 8.To which of the following class does a CNF-satisfiability problem belong? (a) NP class (b) P class (c) NP complete (d) NP hard 9. Which of the following problems is not NP complete? (a) Hamiltonian circuit (b) Bin packing (c) Partition problem (d) Halting problem 10. The choice of polynomial class has led to the development of an extensive theory called (a) computational complexity (b) time complexity (c) problem complexity (d) decision complexity 11.Hamiltonian path problem is _____ (a) NP problem (b) N class problem (c) P class problem (d) NP complete problem 12. Subset sum problem is an example of NP-complete problem. (a) true (b) false 13. What is a subset sum problem? (a) finding a subset of a set that has sum of elements equal to a given number (b) checking for the presence of a subset that has sum of elements equal to a given number and printing true or false based on the result (c) finding the sum of elements present in a set (d) finding the sum of all the subsets of a set 14.What is the set partition problem? (a) finding a subset of a set that has sum of elements equal to a given number (b) checking for the presence of a subset that has sum of elements equal to a given number (c) checking whether the set can be divided into two subsets of with equal sum of elements and printing true or false based on the result (d) finding subsets with equal sum of elements 15.Set partition problem is an example of NP complete problem. (a) true (b) false 16. Describe optimization and decision problem. 17. Describe P and NP – class problem. 18. State Cook's Theorem. 19. Explain the different ways to analyze randamize algorithm. 20. Explain the need of approximation algorithm.